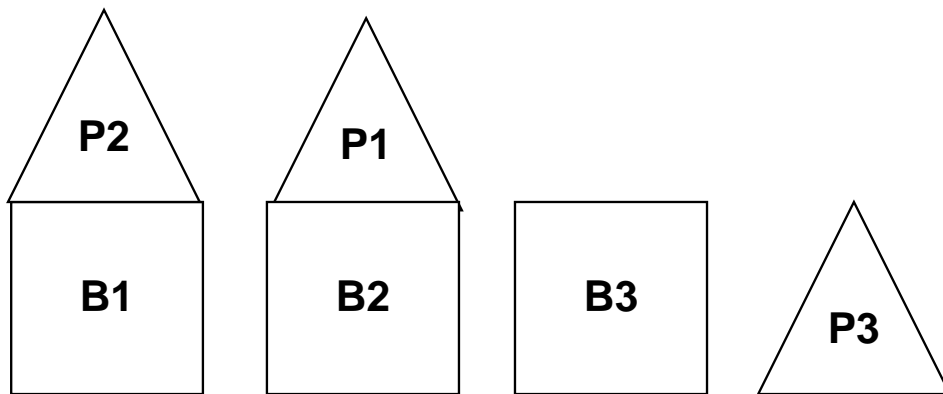


**Exercises for the group exercise session on  
May 8, 1998**

1. Assume that the blocks world is augmented to include three cubes and three pyramids. Give a complete interpretation which characterizes the state shown below.



Use the example on page 14 of the notes on first-order logic as a guide. Give in particular:

- (i) The domain of the interpretation.
  - (ii) The values under the interpretation of the constant symbols B1, B2, B3, P1, P2, and P3.
  - (iii) The values under the interpretation of the relation symbols Is\_cube, Is\_pyramid, On, and On\_table.
2. Assuming that the set of variables is  $\{x_0, x_1, x_2, \dots\}$ , give three distinct valuations for the interpretation which is your answer to question 1. Include two valuations which differ only on the value for  $x_0$ .
  3. For the sentence below, do the following;
    - (a) Draw the parse tree.
    - (b) Identify all instances of bound, shadowed, and free variables.
    - (c) Rename variables to obtain an equivalent formula in which no shadowing occurs, and in which no variable is associated with more than one quantifier.

$$(\forall x)((\forall z)(P(x,y) \wedge (\forall x)(\forall y)R(x,y)) \rightarrow (P(x,y) \vee (\forall y)Q(x,y,z)))$$

4. Work through Exercises 9.2 and 9.3 on page 193 of the textbook. Make sure in particular that you understand why the implications work in one direction but not the other.