Logic with Applications Spring 1998b

Problems for the group exercise session on April 7, 1998

Note: There may not be time to do all of these exercises in the time allotted. If there is one which gives you particular difficulty, come prepared to ask about it.

- 1. Do exercise 5.2 on page 98 of the text.
- 2. Convert each of the formulas of Exercise 5.2 on page 98 of the text to DNF.
- 3. Do problems 1-3 on page 111 of the text. All resolution proofs should be refutation proofs. Also, try to find unit refutation and input refutation proofs, whenever possible.
- 4. For problem 3 on page 111, also provide solutions using the method of semantic tableaux.
- 5. Using resolution, prove that the following sets of clauses are unsatisfiable. To keep things manageable, delete superclauses as the resolution process proceeds.
- (a) { $P \lor \neg R, Q \lor \neg R, Q \lor \neg S, \neg P \lor T, \neg Q \lor \neg T, \neg Q \lor R \lor T, P \lor S \lor \neg T,$ $\neg P \lor Q \lor R, Q \lor R \lor S \lor T$
- (b) { $P \lor \neg R, Q \lor \neg R, \neg P \lor S, \neg P \lor T, \neg Q \lor \neg T, \neg Q \lor R \lor T, P \lor R \lor \neg S,$ $P \vee S \vee \neg T, R \vee \neg S \vee \neg T, Q \vee R \vee S \vee T \}$
- 6. Find the base of the set consisting of the following set of clauses, together with all of its resolvents.

$$\{\neg A \lor B, \neg B \lor C, \neg C \lor \neg D, A \lor D, \neg A \lor B \lor C\}$$