# 5DV118 <br> Computer Organization and Architecture Umeå University Department of Computing Science 

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Topic 3aux: Logic Design

## A Ridiculously Brief Overview of Combinational Logic Design

- These slides provide a brief overview of combinational logic.
- They are limited to the ideas absolutely needed for the course.
- For a more detailed presentation consult Appendix C on the CD which comes with the course text.


## Types of Logic Circuits

- Combinational logic is used to realize memoryless functions.
- Sequential logic is used to realize functions which have an internal state.
- These slides focus upon combinational logic.


## Basic Gates

The AND gate


| $A$ | $B$ | $C$ |
| :---: | :---: | :---: |
| 0 | 0 | 0 |
| 0 | 1 | 0 |
| 1 | 0 | 0 |
| 1 | 1 | 1 |

The Inverter
$A \rightarrow B-B$

| $A$ | $B$ |
| :---: | :---: |
| 0 | 1 |
| 1 | 0 |

The OR gate


| $A$ | $B$ | $C$ |
| :---: | :---: | :---: |
| 0 | 0 | 0 |
| 0 | 1 | 1 |
| 1 | 0 | 1 |
| 1 | 1 | 1 |

The Buffer


| $A$ | $B$ |
| :---: | :---: |
| 0 | 0 |
| 1 | 1 |

## Further Gates

The NAND gate


| A | B | C |
| :---: | :---: | :---: |
| 0 | 0 | 1 |
| 0 | 1 | 1 |
| 1 | 0 | 1 |
| 1 | 1 | 0 |

The XOR gate


| $A$ | $B$ | $C$ |
| :---: | :---: | :---: |
| 0 | 0 | 0 |
| 0 | 1 | 1 |
| 1 | 0 | 1 |
| 1 | 1 | 0 |



| $A$ | $B$ | $C$ |
| :---: | :---: | :---: |
| 0 | 0 | 1 |
| 0 | 1 | 0 |
| 1 | 0 | 0 |
| 1 | 1 | 0 |

## Compact Representation of Negation

- Negation may be represented as a circle on another gate.
- The following two circuits are equivalent.



## The Multiplexer

- A multiplexer selects between two (or more) inputs.
- $S$ is the select line.
- Shown is a two-input multiplexer.


5DV118 t3:aux sl:7 2011-11-16

## A One-Bit Half Adder

| $A$ | $B$ | $S$ | $C$ |
| :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0 |
| 0 | 1 | 1 | 0 |
| 1 | 0 | 1 | 0 |
| 1 | 1 | 0 | 1 |



## A One-Bit Full Adder

| $A$ | $B$ | $C_{\text {in }}$ | $S$ | $C_{\text {out }}$ |
| :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0 | 0 |
| 0 | 1 | 0 | 1 | 0 |
| 1 | 0 | 0 | 1 | 0 |
| 1 | 1 | 0 | 0 | 1 |
| 0 | 0 | 1 | 1 | 0 |
| 0 | 1 | 1 | 0 | 1 |
| 1 | 0 | 1 | 0 | 1 |
| 1 | 1 | 1 | 1 | 1 |

Carry in


Carry out

## A Sequential Adder

- An n-bit sequential adder may be realized by gluing $n$ one-bit adders together.
- This is not the best design because the critical path is proportional to n .


Carry out

